

```
> restart :
> interface(warnlevel=0) :          # Maple 12
> with(LinearAlgebra) :
```

Chapter 7 Problem 2b

The eigenvalues and eigenvectors of the Pauli Matrices

```
> X := RowOperation(IdentityMatrix(2), [2, 1]);
```

$$X := \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \quad (1)$$

Determining the eigenvalues and eigenvector of a matrix using Maple's Eigenvectors() function

```
> L := Eigenvectors(X) :      # a list of the eigenvalues with their corresponding eigenvectors
print(eigenvalue=L[1][1], eigenvector=L[2][1..2, 1], magnitude=Norm(L[2][1..2, 1], Euclidean));
print(eigenvalue=L[1][2], eigenvector=L[2][1..2, 2], magnitude=Norm(L[2][1..2, 2], Euclidean));
```

$$\begin{aligned} \text{eigenvalue} = 1, \text{eigenvector} &= \begin{bmatrix} 1 \\ 1 \end{bmatrix}, \text{magnitude} = \sqrt{2} \\ \text{eigenvalue} = -1, \text{eigenvector} &= \begin{bmatrix} -1 \\ 1 \end{bmatrix}, \text{magnitude} = \sqrt{2} \end{aligned} \quad (2)$$

```
> Y := Matrix([ [0, -I], [I, 0]]);
L := Eigenvectors(Y) :      # a list of the eigenvalues with their corresponding eigenvectors
print(eigenvalue=L[1][1], eigenvector=L[2][1..2, 1], magnitude=Norm(L[2][1..2, 1], Euclidean));
print(eigenvalue=L[1][2], eigenvector=L[2][1..2, 2], magnitude=Norm(L[2][1..2, 2], Euclidean));
```

$$\begin{aligned} Y &:= \begin{bmatrix} 0 & -I \\ I & 0 \end{bmatrix} \\ \text{eigenvalue} = 1, \text{eigenvector} &= \begin{bmatrix} -I \\ 1 \end{bmatrix}, \text{magnitude} = \sqrt{2} \\ \text{eigenvalue} = -1, \text{eigenvector} &= \begin{bmatrix} I \\ 1 \end{bmatrix}, \text{magnitude} = \sqrt{2} \end{aligned} \quad (3)$$

```
> Z:=Matrix([ [1, 0], [0, -1]]);
```

```
L:=Eigenvectors(Z) :    # a list of the eigenvalues with their corresponding eigenvectors  
print(eigenvalue=L[1][1], eigenvector=L[2][1..2, 1], magnitude=Norm(L[2][1..2, 1], Euclidean));  
print(eigenvalue=L[1][2], eigenvector=L[2][1..2, 2], magnitude=Norm(L[2][1..2, 2], Euclidean));
```

$$Z:=\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$$

$$\text{eigenvalue} = 1, \text{eigenvector} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}, \text{magnitude} = 1$$

$$\text{eigenvalue} = -1, \text{eigenvector} = \begin{bmatrix} 0 \\ 1 \end{bmatrix}, \text{magnitude} = 1$$

(4)